

NUMERICAL STUDY OF THE INFLUENCE OF HEAVY DOPING EFFECTS ON THE CURRENT GAIN OF N-P-N POWER TRANSISTORS

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in Partial Fulfilment of the Requirements
for the Degree of**

MASTER OF TECHNOLOGY

BY

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to the

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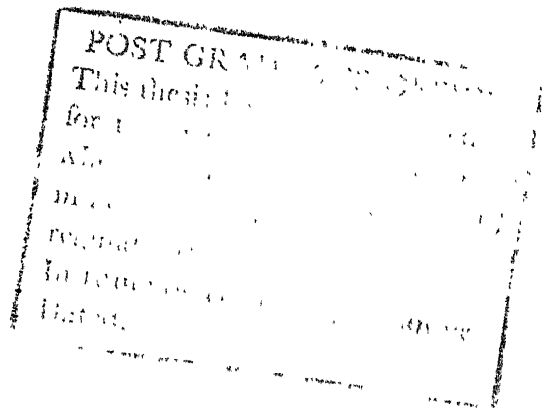
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C E R T I F I C A T E

This is to certify that the work entitled 'NUMERICAL STUDY OF THE INFLUENCE OF HEAVY DOPING EFFECTS ON THE CURRENT GAIN OF N-P-N POWER TRANSISTORS' has been carried out by Mr. A.V. Chaturvedi under my supervision and this has not been submitted elsewhere for a degree.

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A C K N O W L E D G E M E N T S

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LIST OF SYMBOLS

x_{je}, x_{jc}	- location of emitter-base/base collector junction from the surface of the transistor.
V_T	- Thermal voltage at 300°K.
D_o	- Diffusion constant
L_p	- Diffusion length
n_{ie}	- correction factor to the intrinsic carrier concentration.
Ψ, V	- electrostatic potential, applied voltage
q	- electronic charge
ϵ	- permittivity
p, n, N	- concentration of holes, electrons, ionized impurities.
J_p, J_n, J_T	- hole, electron, Total current density
R	- recombination rate
G	- generation rate
n_i	- Intrinsic carrier concentration
k	- Boltzman constant
T, T_o	- Temperature, 300°K
ϕ_n, ϕ_p	- electron, hole quasi-Fermi potentials
μ_p, μ_n	- hole, electron mobilities
E	- Electric field
R_1	- SRH recombination rate
R_2	- Auger recombination rate

τ_{po}, τ_{no}	- equilibrium hole, electron lifetime
δ	- change in the potential
ψ^{new}	- corrected value of potential
u	- general variable
h	- distance between two successive step points
A	- coefficient matrix
X	- unknown vector
Q	- source term vector
b_m	- the terms on subdiagonal of A
c_m	- the terms on diagonal of A
d_m	- the terms on supradiagonal of A
N_E, N_C, N_B	- emitter, collector, base surface concentration
α	- profile parameter
β	- profile parameter
A_n, A_p	- Auger Coefficients for electron/hole
α_n, α_p	- high field generation coefficients for electron/hole
A_E	- emitter area
W_C	- length of considered collector region
τ_b, τ_c, τ_e	- Lifetime of carriers in base/collector/emitter.
N_D^+, N_A^-	- ionized donor/acceptor atom density.

A B S T R A C T

The heavy doping phenomenons of bandgap narrowing and Auger recombination have been numerically modeled. Their individual and relative importance in determining the current gain of an n-p-n power transistor have been studied. It is shown that in the devices with emitter junction depths of $2\mu\text{m}$ or less bandgap narrowing dominates all other mechanisms. SRH recombination has the most effect on current gain in the devices with emitter junction depths of $4\mu\text{m}$ or more.

CHAPTER 1

INTRODUCTION

The operation of a junction transistor depends on the introduction and transport of minority carriers across the base region of the transistor. In the design of an efficient transistor, it is necessary to contrive that the emitter current is predominantly a current of minority carriers emitted into the base rather than a current of majority carriers withdrawn from the base. For this requirement to be met the emitter side of the emitter base junction must be more heavily doped than the base side.

In most silicon devices, the emitter doping levels in excess of 10^{18} cm^{-3} are found. At such high doping levels, the basic parameters such as the density of states, the width of the forbidden energy gap, the minority carrier mobility and the minority carrier lifetime strongly differ from their values in a lowly doped crystal. The bandgap of silicon is reduced, the electron and hole mobilities decrease and the minority carrier lifetime becomes lower at heavy doping levels.

These heavy doping effects have to be taken into account in the modeling of transistor. The electron and hole mobilities in silicon as a function of dopant concentration and temperature are important parameters for device

design and analysis. The importance of the minority carrier lifetime is obvious. It influences dc as well as transient performance. The impact of bandgap narrowing effects on device performance is nearly as obvious. The bandgap shrinkage and the deformation of band structure results in an increase in the pn product with increasing impurity concentration. Keeping in mind that most electrical quantities of interest, such as currents and minority carrier storage, are proportional to this product one understands the impact of these effects on the device performance. Heavy emitter doping has a detrimental effect on many transistor parameters. In addition to decreasing the transistor gain and increasing the temperature dependence of gain, it also results in a higher noise figure. The excess noise generally attributed to surface effects is substantially larger for heavily doped emitters.

1.1 Literature Survey :

Mertens et al^{[1],[2]} have considered the heavy doping effects by modifying the device transport equations. They have calculated the transistor current gain after solving numerically these modified transport equations. Slotboom et al^[3] have given an empirical formula for bandgap shrink-

lage, which can be used for concentrations in the range of $4 \times 10^{15} - 2.5 \times 10^{19} \text{ cm}^{-3}$. Lanyon et al^[4] have derived an analytical expression for bandgap narrowing which may be used for modeling of the bandgap shrinkage. The expression is in good agreement with experimental results in the doping range of 3×10^{17} to $1.5 \times 10^{20} \text{ cm}^{-3}$. Possin et al^[5] have suggested some modification in the classical device equations for including the bandgap narrowing. They suggest using an effective electric field term in the equations. Gaur et al^[6] have modeled the heavy doping effects by including Auger recombination and correction to intrinsic carrier concentration. The results of measurements of bandgap narrowing done by a number of investigators is shown in Fig. 1.

Shibib et al^[7] have shown that Auger recombination alone cannot explain the common emitter current gain in bipolar transistors. Other physical mechanisms in addition to Auger recombination have to be considered to account for the observed values of current gain. The Auger coefficients calculated by various authors are tabulated in Table 1. Numerical treatment of Auger recombination has been done by [8 - 10]. Recently Polsky et al^[11] have numerically simulated the bipolar semiconductor devices taking into account heavy doping effects and Fermi statistics.

1.2 Preview :

The objective of the present work is to simulate the heavy doping effects of bandgap narrowing and Auger recombination in order to determine their individual and relative influence on the current gain of an n-p-n power transistor. The basic device equations in one dimension with required modification for inclusion of bandgap narrowing and Auger recombination effects, have been solved for the transistor and its current gain for the given impurity profile has been determined in the presence of different combinations of these effects. Chapter two presents the physical basis for the modeling. Chapter three discusses first the general philosophy of modeling and various approaches to the modeling of bipolar devices. The approach followed for the modeling of n-p-n power transistor is then described. Chapter four presents the results obtained and the discussion of the results. Plots of current gain versus emitter junction depths and current gain versus collector currents are presented. Chapter five summarizes the main results of the work. The computer programmes written in Fortran have been included in the Appendix.

CHAPTER 2

THEORATICAL BACKGROUND

2.1 Energygap :

At heavy doping levels, the number of mobile carriers is very large and they are quantum mechanically indistinguishable i.e. one particle cannot be distinguished from the other. The energy distribution of carriers in such conditions obey the Fermi-Dirac statistics rather than Maxwell-Boltzman statistics which is obeyed at lower doping levels when the particles are distinguishable.

Since there is a large number of carriers in the crystal, the separation between them is very small and the interaction between carriers, and carriers and ionized ions becomes prominent. The majority electrons (for n-type Si) screen the donor ions through Columb interaction and reduce the ionization energy of the donor. This results in donor level moving up toward and ultimately into the conduction band. Similarly, when majority electrons interact with minority holes, the hole potential energy is reduced and the valence band edge moves toward conduction band. The electron-electron interaction is due to their spin motion and there is an exchange energy associated with this motion. The effect of this interaction on energy band is that the conduction band edge moves downward.

The distribution of impurity atoms in the crystal at heavy dopings is not uniform. The crystal is disordered and the distribution of donor ions is random. This random distribution causes fluctuations in local electrostatic potential and variations in the energy of the electronic states in both the conduction and valence band results. These variations in energy cause a spatially dependent distortion of quantum density of states. Concomittantly the statistical average over the entire lattice, of the density of states, which defines the macroscopic properties of the semiconductor, shows tailing into the energy gap, of both the conduction and valence band density of states. The bands are not parabolic near the extrema in such cases and the energy gap is effectively reduced.

The discrete donor levels at low dopings levels, spread to form a band at high doping levels. This is because the spacing between the impurity atoms is small. This allows the electron wave function at the bound states to overlap. The random distribution of the donors also results in variation in the donor energy level and formation of impurity band tails. The effect of the impurity band formation on band structure is negligible since the impurity bands are narrow, there is only a small number of electrons in them, and the mobility of these electrons is small.

The measurements of bandgap narrowing have yielded two types of bandgaps. The measurement of optical absorption give the 'optical' energy gap. The change in this bandgap is due to many body effects such as the interaction of electrons with electrons, and with holes. The measurements of minority carrier concentrations yield the 'electrical' energy gap. The change in this gap is due to both many body effects and band tailing effects. This change in 'electrical' energy gap defines the effective intrinsic carrier density n_{ie} .

2.2 Auger Recombination :

The band-to-band Auger recombination is a three carrier effect. In this process, the recombining e-h pair gives its energy either to an electron in the conduction band (called e-e-h process) or to a hole in the valence band (called e-h-h process). The Auger recombination predicts lifetime inversely proportional to the square of the majority carrier concentration in degenerate as well as in non-degenerate semiconductors.

CHAPTER 3

DEVICE MODELING

Modeling is the art of characterization of the behaviour of a physical process. The device model attempts to describe the internal and the terminal electrical behaviour of the device. There are two broad categories into which modeling can be divided. Both these approaches are commonly used in device modeling. The parameters of an empirical model are generally obtained through a study of the experimentally measured behaviour of the device as viewed from its terminals. This involves application of curve fitting techniques to obtain functional relationships between the terminal quantities of interest. The physical model, on the other hand, is based on an analysis of the basic internal physical mechanism of the device. It enables an insight into the working of the device and gives an excellent qualitative picture of the effects of changes in material and structural parameters on its terminal, electrical behaviour.

Models have also been developed which make use of a combination of the two approaches mentioned above. The physics of the device is used as a guide to its terminal description. As far as the device engineer is concerned, it is the physically oriented model that is more important.

This is because only this type of model enables the optimization-designing the device so as to improve some specific aspect of circuit performance to be performed.

3.1 Transistor Modeling :

The following three basic approaches are in use for modeling a transistor.

- (a) The classical analytic approach : The models developed using this approach are simple, can be analytically manipulated, and are directly related to the physics of the device. However, they do not accurately represent the behaviour of the device under all conditions of operation. An example of this type of approach is the well-known Shockley model of a transistor.
- (b) The total computer approach : This approach is based on a rigorous solution of the basic semiconductor equations. The results obtained are highly accurate.
- (c) The regional approximation method : This approach is based on the division of the transistor structure into well-defined physical regions. Different approximation are made on the basic semiconductor equations in the different regions and these equations are then solved either analytically or

on the computer. The self-consistency of the approximation is checked from point to point.

The present modeling follows the total computer approach. The basic semiconductor equations are solved by finite difference method after including modifications due to heavy doping concentrations. The bandgap narrowing is modeled as correction to the intrinsic carrier concentration and the modeling of Auger recombination is done by adding an expression of Auger recombination rate to the expression of SRH recombination. For mobilities expressions are used for its dependence upon carrier concentration and electric field.

3.2 Problem Definition :

The problem is to obtain current gain of an n-p-n power transistor with varying emitter junction depths by solving a set of three basic semiconductor device equations, introduced in the next section. The following information about the device is given; geometry, doping profile, mobilities as function of electric field and impurity density, generation recombination laws including Auger recombination, intrinsic carrier concentration corrected for bandgap narrowing and the appropriate boundary conditions.

3.3 Basic Equations :

The semiconductor transport equations which have to be solved for the steady state behaviour under isothermal conditions are

$$\nabla^2 \Psi = - \frac{q}{\epsilon} (p - n - N) \quad (1)$$

$$\nabla \cdot J_p = - q(R - G) \quad (2)$$

$$\nabla \cdot J_n = + q(R - G) \quad (3)$$

$$J_p = - q \mu_p p \nabla \Psi - q D_p \nabla p \quad (4)$$

$$J_n = - q \mu_n n \nabla \Psi + q D_n \nabla n \quad (5)$$

$$J_T = J_p + J_n \quad (6)$$

Equation (1) is the Poisson's equation, relating the divergence of the electric flux to the electrostatic charge due to mobile holes (p) and electrons (n) and the ionized impurity atom density ($N = N_D^+ - N_A^-$). The Equations (2) and (3) are the continuity equations for the holes and electrons under steady state conditions. Equations (4) and (5) are the current density relations composed of drift (due to the electric field) and diffusion (due to carrier concentration

gradient) terms. Boltzman approximation of Fermi statistics between the potential and carrier densities have been assumed.

$$n = n_i \exp \left(q \frac{(\psi - \phi_n)}{kT} \right) \quad (7)$$

$$p = n_i \exp \left(q \frac{(\phi_p - \psi)}{kT} \right) \quad (8)$$

Quantities ϕ_p and ϕ_n in Equations (7) and (8) represent hole and electron quasi-Fermi potentials. The Einstein relation between the carrier mobilities and the diffusion coefficients are assumed to be valid, although this cannot be done for majority carriers in degenerate semiconductors. The dependence of carrier mobilities on electric field and impurity atom density is modeled according to the following formula.^[25]

$$\left(\frac{480}{\mu_p} \right)^2 = 1 + \frac{N}{(N/81) + 4 \times 10^{16}} + \frac{(E/6.1 \times 10^3)^2}{(E/6.1 \times 10^3) + 1.6} + \left(\frac{E}{9.5 \times 10^4} \right)^2 \quad (9)$$

$$\left(\frac{1400}{\mu_n}\right)^2 = 1 + \frac{\frac{N}{350} + \frac{N}{3 \times 10^{16}}}{\frac{(\frac{E}{3.5 \times 10^3})^2}{(\frac{E}{3.5 \times 10^3}) + 8.8}} + \left(\frac{E}{7.4 \times 10^3}\right)^2 \quad (10)$$

The Shockley-Read-Hall recombination law is given as follows

$$R1 = \frac{p_n - n_i^2}{\tau_{no}(p+n_i) + \tau_{po}(n+n_i)} \quad (11)$$

The equations for the Auger recombination and high field generation rate are the following

$$R2 = (A_n n + A_p p)(p_n - n_i^2) \quad (12)$$

$$G = n \mu_n \alpha_n E + p \mu_p \alpha_p E \quad (13)$$

The values of various constants entering the equations (12) and (13) are given in Table 2. [6]

The transport equations (1) - (6) are normalized into **dimensionless** forms according to normalization factors of Table 3. The normalized set of equation is reduced to three coupled equations in variables Ψ , n and p .

$$\nabla^2 \Psi = n - p - N \quad (14)$$

$$\nabla \cdot (\mu_p (p \nabla \Psi + \nabla p)) = R - G \quad (15)$$

$$\nabla \cdot (\mu_n (n \nabla \Psi - \nabla n)) = R - G \quad (16)$$

Equations (7) and (8) in their normalized form reduce to

$$n = \exp (\Psi - \phi_n) \quad (17)$$

$$p = \exp (\phi_p - \Psi) \quad (18)$$

Here two variables $\bar{\phi}_p$ and $\bar{\phi}_n$ are explicitly introduced

$$\bar{\phi}_p = \exp (\phi_p) \quad (19)$$

$$\bar{\phi}_n = \exp (-\phi_n) \quad (20)$$

These expressions are substituted in the equations (14), (15) and (16) to obtain a new set of equations in the variables Ψ , $\bar{\phi}_p$ and $\bar{\phi}_n$

$$\nabla^2 \Psi = \bar{\phi}_n \exp(\Psi) - \bar{\phi}_p \exp(-\Psi) - N \quad (21)$$

$$\nabla \cdot (\mu_p \exp(-\Psi) \nabla \bar{\phi}_p) = R - G \quad (22)$$

$$\nabla \cdot (\mu_n \exp(\Psi) \nabla \bar{\phi}_n) = R - G \quad (23)$$

These three coupled equations have been solved by the method outlined next.

3.4 Discretization :

The Poisson's equation (21) is nonlinear in Ψ . This is linearized by assuming

$$\Psi^{\text{new}} = \Psi + \delta \quad (24)$$

where Ψ is the potential value of the previous iteration and δ is the correction term. We have

$$\begin{aligned} \nabla^2 \Psi + \nabla^2 \delta &= \bar{\rho}_n \exp(\Psi + \delta) - \bar{\rho}_p \exp(-\Psi - \delta) - N \\ &= \bar{\rho}_n \exp(\Psi) [1 + \delta + O(\delta^2)] - \bar{\rho}_p \exp(-\Psi) [1 - \delta + O(\delta^2)] - N \\ &= \bar{\rho}_n \exp(\Psi) - \bar{\rho}_p \exp(-\Psi) - N + \delta (\bar{\rho}_n \exp(\Psi) + \bar{\rho}_p \exp(-\Psi)) \end{aligned}$$

$$\therefore \nabla^2 \delta - \delta (\bar{\rho}_n \exp(\Psi) + \bar{\rho}_p \exp(-\Psi)) = -\nabla^2 \Psi + \bar{\rho}_n \exp(\Psi) - \bar{\rho}_p \exp(-\Psi) - N \quad (25)$$

Thus neglecting the second and higher order terms equation (25) is considered as a linear differential equation for δ .

The discretization process is achieved with the selection of a uniform step distribution. The finite difference scheme used for reducing the Poisson's equation to the equivalent linear algebraic equation replaces the first derivative at the i^{th} step by the formula

$$\left. \frac{du}{dx} \right|_i = \frac{u_{i+1} - u_{i-1}}{2h} \quad (26)$$

and the second derivative by

$$\left. \frac{d^2u}{dx^2} \right|_i = \frac{u_{i+1} + u_{i-1} - 2u_i}{2h^2} \quad (27)$$

where u_{i+1} , u_{i-1} , u_i and h are the values of the function is at points $i+1^{\text{th}}$, $i-1^{\text{th}}$, i^{th} and the distance between two successive points, respectively. Using these formulas, the difference equation at the point 'i' [Fig. 2] is written as

$$\begin{aligned} [2 + h^2 (\phi_n(i) \exp(\Psi(i)) + \phi_p(i) \exp(-\Psi(i)))] \delta_i \\ = \delta_{i+1} + \delta_{i-1} + \Psi_{i+1} + \Psi_{i-1} - 2\Psi_i - h^2 (\phi_n(i) \exp(\Psi(i)) \\ - \phi_p(i) \exp(-\Psi(i)) - N(i)) \end{aligned} \quad (28)$$

The continuity equations are replaced by the difference equation which are obtained by the box integration method.

The difference equation corresponding to the equation (22) is given as follows

$$\begin{aligned} (a(i+\frac{1}{2}) + a(i-\frac{1}{2})) \bar{\phi}_p(i) = a(i+\frac{1}{2}) \bar{\phi}_p(i+1) + a(i-\frac{1}{2}) \bar{\phi}_p(i-1) \\ - h^2 (R_i - G_i) \end{aligned} \quad (29)$$

where $a = \mu_p \exp(-\Psi)$

The value of 'a' at the point midway between two successive step points is approximated from the known

values of 'a' at these two points. The difference equation for the relation (23) is similar to (29), but with $a = \mu_n \exp(\Psi)$.

3.5 Solution Procedure :

The difference equations derived in the last section are applied to every point of the step distribution which give rise to a system of simultaneous algebraic equations. These equations can be written in a matrix form as follows

$$AX = Q \quad (30)$$

This matrix equation represents a system of linear equations where each component of the unknown vector 'X' is related only to adjacent components.

$$b_m x_{m-1} + a_m x_m + d_m x_{m+1} = Q_m \quad (31)$$

The matrix thus formed is of triple-diagonal form. The matrix equation is solved directly by a method known as Crout's method. It is a numerical procedure for forward elimination followed by backward substitution. The recursion formulas for the technique are as follows :

$$\left. \begin{aligned} x_n &= p_n \\ x_m &= p_m + h_m x_{m-1} \quad m=n-1, n-2, \dots, 1 \end{aligned} \right\} \quad (32)$$

where

$$\left. \begin{aligned} h_m &= \frac{-d_m}{c_m + b_m h_{m-1}}; & h_1 &= -\frac{d_1}{c_1} \\ p_m &= \frac{Q_m - b_m p_{m-1}}{c_m + b_m h_{m-1}}; & p_1 &= \frac{Q_1}{c_1} \end{aligned} \right\} \quad (33)$$

The sequence of solution for Ψ , φ_p and φ_n is similar to the one described in reference [12] and is called Gummel's algorithm Fig. (3).

1. An initial guess to Ψ is made from which initial values of φ_p and φ_n are calculated for the given applied voltage.
2. Poisson's equation is solved and new value of Ψ is calculated.
3. Continuity equations are solved to obtain new values of φ_p and φ_n .
4. A test of accuracy is done. If required accuracy is reached the iteration is stopped **otherwise** go back to step 2.

The current gains are calculated as the ratios of collector current and base terminal current. The effect of

various physical mechanisms with varying emitter size is incorporated by doing the calculation on the above mentioned lines with emitters of different sizes. For this type of computations the total emitter charge is kept constant as the emitter depth is varied.

CHAPTER 4

RESULTS AND DISCUSSION

4.1 Results

The calculations were performed for a power transistor structure which has the following double Gaussian doping profile.

$$N(x) = N_E e^{-\alpha(x/x_{je})^2} + N_C - N_B e^{-\beta(x/x_{je})^2} \quad (34)$$

where the distance x is measured from the surface of the transistor. The structural and profile parameters of the transistors studied are given in Table [4]. Fig. [4] is a plot of the doping profile.

The material parameters of the transistor are given in Table [5].

The determination of the emitter surface concentration required for equal emitter charge for varying emitter junction depths was done using programme (2).

The results of the calculations performed for the determination of relative importance of various physical phenomena by varying the emitter depth are tabulated in Table [6] and shown on Fig. (5).

The results of the computations performed for the determination of current gain variation with collector current

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in the presence of different physical mechanisms are reported in Table 7 and plotted in Fig. (6).

4.2 Discussion

Fig.(5) shows the dependence of current gain on emitter junction depths in the presence of different combinations of physical processes. The current level in all cases is 8.2A/cm^2 . First, the case of $4\mu\text{m}$ device is considered since it is typical of the overall results. The current gain in the situation when all the mechanisms are contributing, is just below 100. If bandgap narrowing is removed now the current gain increases to 140, showing no significant influence of bandgap narrowing for such a device. If bandgap narrowing is restored and emitter SRH traps are removed, the current gain increase to 425. The removal of Auger recombination in combination of any of the other physical phenomenon, produces only a little further change in the current gain. Thus this shows that SRH recombination is the dominant mechanism influencing the current gain of the devices with emitter junction depth in the range of $4\mu\text{m}$. As the junction depth is further increased, the degree of this effect is also increased.

In the case of the devices with emitter depths of $2\mu\text{m}$ or less, the direction of these dependencies is same

but the relative magnitudes change. The bandgap narrowing produces larger changes in the current gain on removal. The SRH recombination has little effect on current in this range.

The dependence of current gain on emitter junction depth in the presence of all mechanisms can now be explained. As the emitter depth is increased from 1 μm to 2 μm the bandgap narrowing effect weakens and therefore current gain increases. In the devices of emitter depths greater than 2 μm , current gain decreases with the depth since the effective emitter charge is lower because the net impurity density is gradually decreasing in the active emitter region near the base region.

Figure (6) shows the variation of current gain with increasing collector current level. Curve (a) shows the same for the case when all mechanisms are operating; Curve (b), when Auger recombination has been removed. Curve (c), when bandgap narrowing has been removed and Curve (d), when bandgap narrowing and Auger recombination both have not been considered in the analysis. It is clear from the Fig. that Auger recombination does not have much influence on the current gain. On removing bandgap narrowing from the analysis, the resulting current gain increases. Removing Auger recombination alone or alongwith bandgap narrowing produces little further change in the current gain.

The importance of SRH recombination in determining current gain can be argued as follows. If there is no recombination, bandgap narrowing has virtually no effect on current gain with increasing injection level. Bandgap narrowing enhances the recombination rate if recombination is occurring and this reduces the current gain. As is obvious from the earlier discussion, this is the main effect of bandgap narrowing in devices with emitter junction depths greater than 4 μm . Auger recombination increases with injection level thus reducing the current gain or at best leaving it unchanged. High injection level effects also tend to reduce the current gain. Contrary to all this, SRH recombination decreases with injection level and thus is the only mechanism that can explain the observed initial rise in the current gain with injection level. Bandgap narrowing can affect the recombination rate but alone cannot explain the observations. These arguments are confirmed by the necessity of adjusting the emitter lifetime at different injection level to correctly predict the current gain.

TABLE 1

Auger Coefficients at 300°K from
studies in heavily doped silicon

Auger Coefficients $\text{cm}^6 \text{sec}^{-1}$		Authors and references
A_n	A_p	
1. 1.7×10^{-31}	1.2×10^{-31}	Beek and Conradt (19)
2. 2.8×10^{-31}	9.9×10^{-32}	Dziwior and Schmidt (20)
3. 1.6×10^{-31}	-	Wieder (18)
4. 5×10^{-32}	-	Weaver and Nasby (21)
5. 4×10^{-32}	-	Possin et al (22)
6. 2×10^{-32}	-	Huldt (23)
7. -	1.7×10^{-31}	Leachman (24)

TABLE 2

Values of Coefficients

A_n	$1.4 \times 10^{-31} \text{ cm}^6 \text{ sec}^{-1}$
A_p	$9.9 \times 10^{-32} \text{ cm}^6 \text{ sec}^{-1}$
α_n	$3.8 \times 10^6 \exp(-1.75 \times 10^6 / E)$
α_p	$2.25 \times 10^7 \exp(-3.2 \times 10^6 / E)$

TABLE 3

Normalization Table

Variable	Normalized quantity	Factor of normalization
Electrostatic Potential	Ψ	$V_t = \frac{kT_0}{q} = .026 \text{ V}$
Quasi-Fermi Levels	φ_n, φ_p	V_t
Voltage	V	V_t
position coordinates	x	$L_D = \sqrt{\frac{\epsilon V_t}{qn_i}} = 34 \mu\text{m}$
Charge Concentrations	$n_i, p, n, N, N_B, N_E, N_C$	$n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$
Carrier Diffusion Coefficients	$\mu_n V_t, \mu_p V_t$	$D_0 = 1 \text{ cm}^2/\text{sec}$
Carrier mobilities	μ_n, μ_p	$\frac{D_0}{V_t} = 39.06 \text{ cm}^2/\text{sec V}$
Current densities	J_T, J_p, J_n	$\frac{qD_0 n_i}{L_D} = 7.05 \times 10^{-7} \text{ A/cm}^2$
Generation recombination rate	R, R_1, R_2, G	$\frac{D_0 n_i}{L_D^2} = 1.3 \times 10^{15} / \text{cm}^3 \text{sec}$
Carrier lifetimes	$\tau_{no}, \tau_{po}, \tau_b, \tau_c, \tau_e$	$\frac{L_D}{D_0} = 34 \times 10^{-4} \text{ sec.}$

TABLE 4

Structural and profile parameters of the transistor

A_B	x_{je}	x_{je}	N_B	N_B	N_C	W_C	α	β
.12 cm ²	4.75x 10 ⁻⁴ cm	12.25x 10 ⁻⁴ cm	7x10 ¹⁹ / cm ³	2x10 ¹⁷ / cm ³	2x10 ¹⁴ / cm ³	77.75x 10 ⁻⁴ cm	7.061	1.2

TABLE 5

Material parameters of the transistor

τ_b	0.5 x 10 ⁻⁶ sec
τ_c	0.5 x 10 ⁻⁶ sec
$\tau_e(\text{low level})$	20 x 10 ⁻⁹ sec
$\tau_e(\text{high level})$	200 x 10 ⁻⁹ sec.

TABLE 6

Current gain for various emitter jn depths.

emitter Jn Depth	All the mechanism contributing	Auger removed	BGN removed	BGN + AR removed	emitter SRH traps removed
	1	2	3	4	5
1μm	104.85	105.97	419.13	421.03	133.21
2μm	118.34	119.23	253.35	255.60	256.73
4μm	99.23	99.55	140.74	142.12	425.19
8μm	55.76	57.31	64.61	65.78	501.25

TABLE 7

Current gain for different collector currents

Collector current (Amp)	1 All present	2 AR removed	3 BGN removed	4 BGN+AR removed
0.3	65.32	64.87	86.23	87.43
0.5	65.04	65.91	88.45	89.85
0.94	70.25	71.30	94.02	95.28
1.60	72.14	73.48	95.26	96.79
1.8	74.39	75.21	97.83	99.12
2.0	75.46	75.89	98.47	99.89
2.4	75.58	76.02	99.14	100.36
3.0	76.14	77.24	100.42	102.01
4.2	76.53	77.63	101.63	103.42
4.8	77.06	78.12	102.45	104.79
5.3	64.30	65.24	88.01	89.81
5.9	53.21	55.61	77.38	79.52
6.3	45.18	46.72	68.12	70.63
7.5	27.41	29.50	51.48	54.21
9.0	17.59	19.32	41.62	43.72

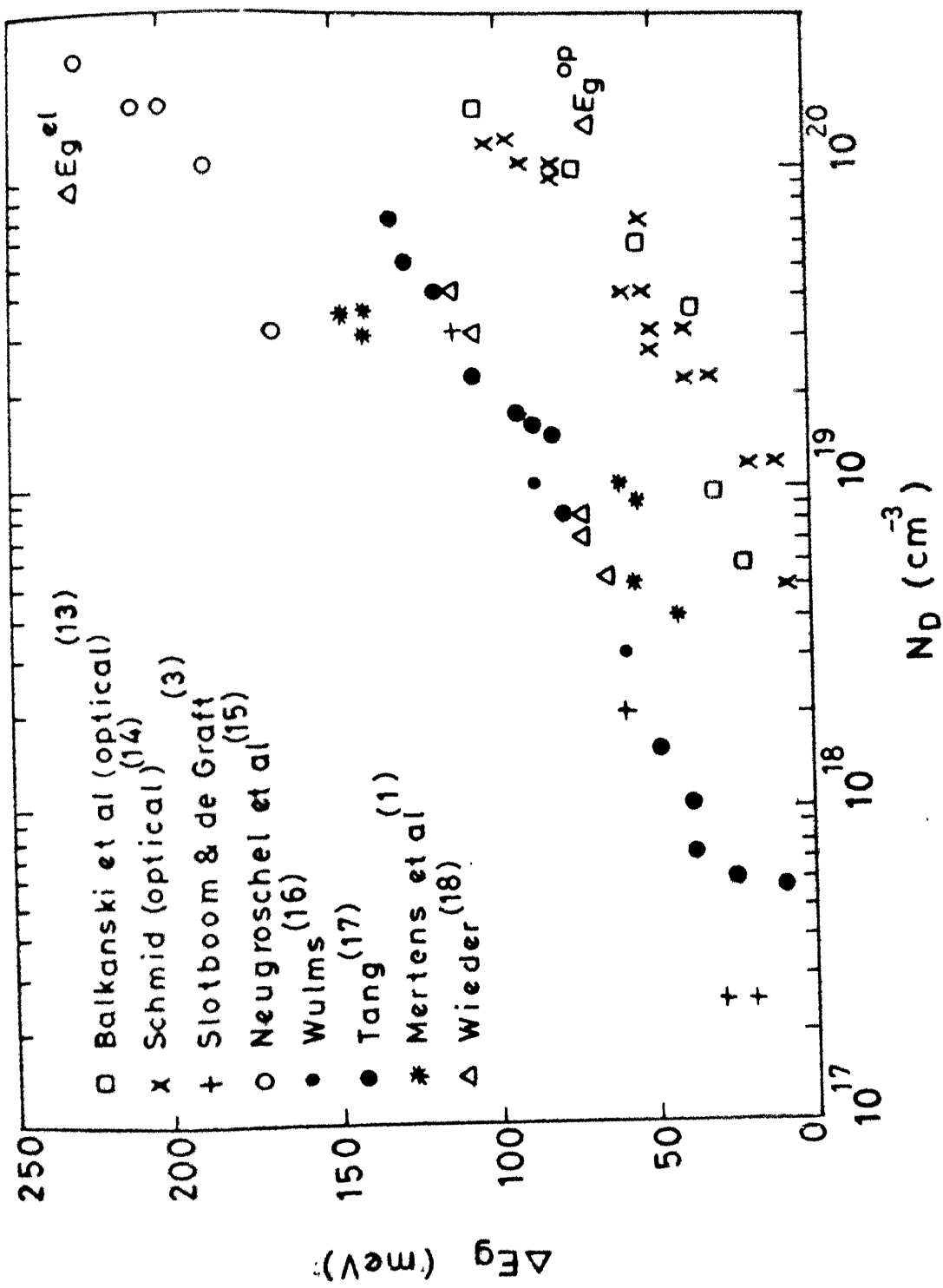


Fig.1 Bandgap narrowing measurements

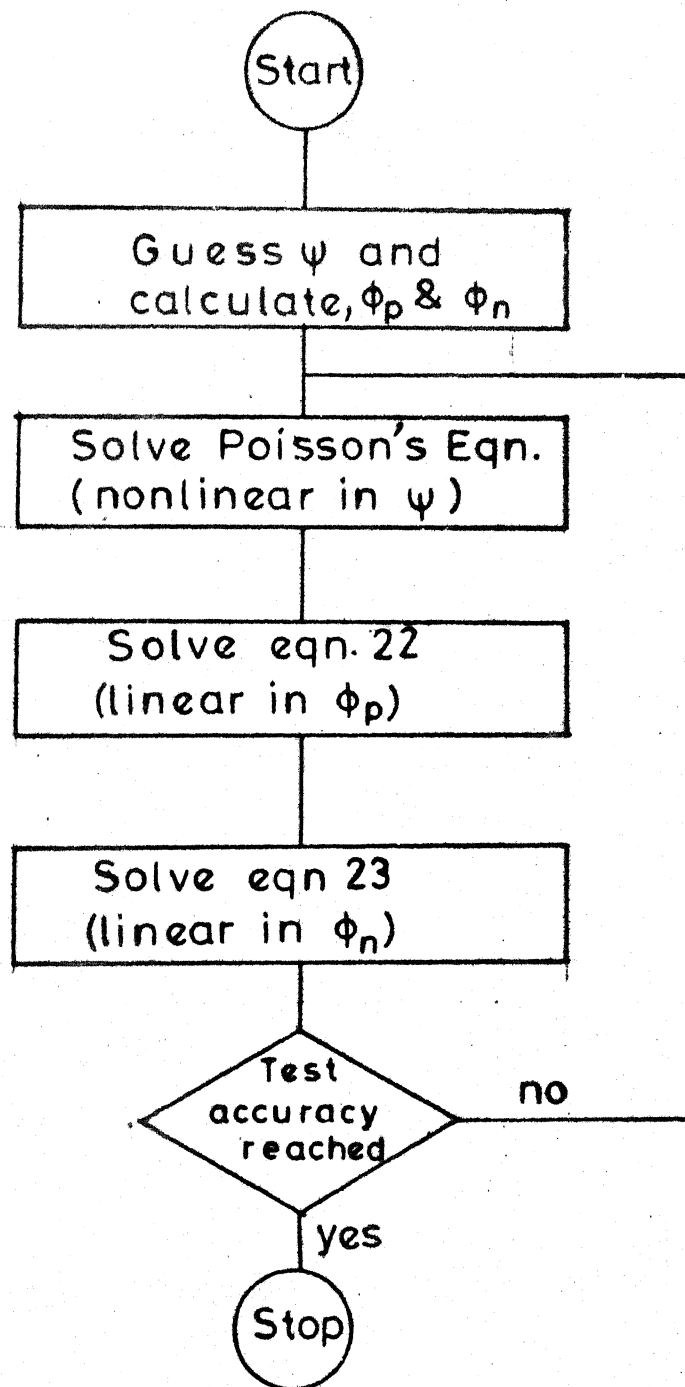


Fig.3 Flow diagram of the solution procedure



Fig.2 Step distribution for discretizing the device equations

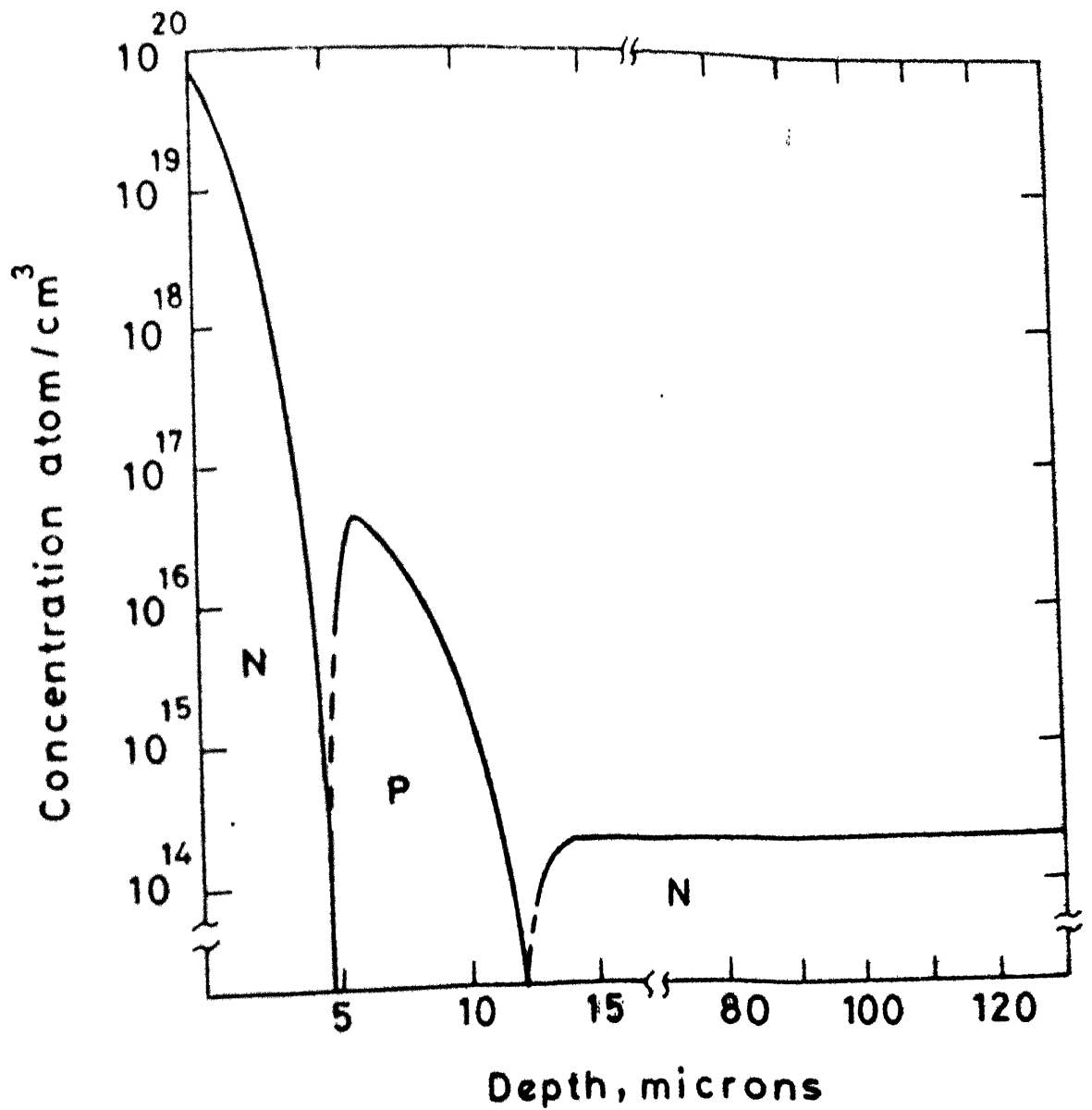


Fig.4 Doping profile for power transistor

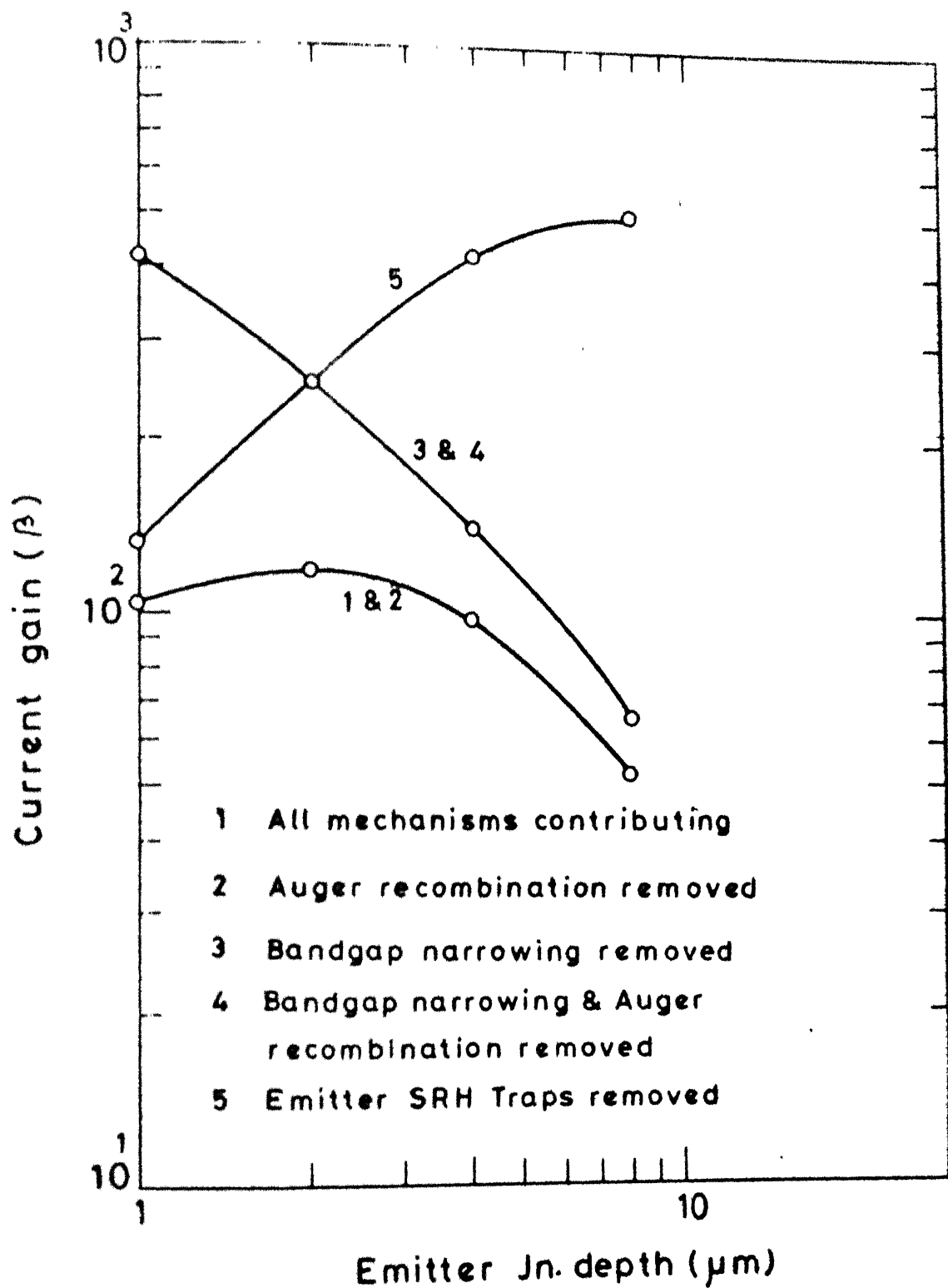


Fig.5 Calculated current gains for different emitter Jn. depths

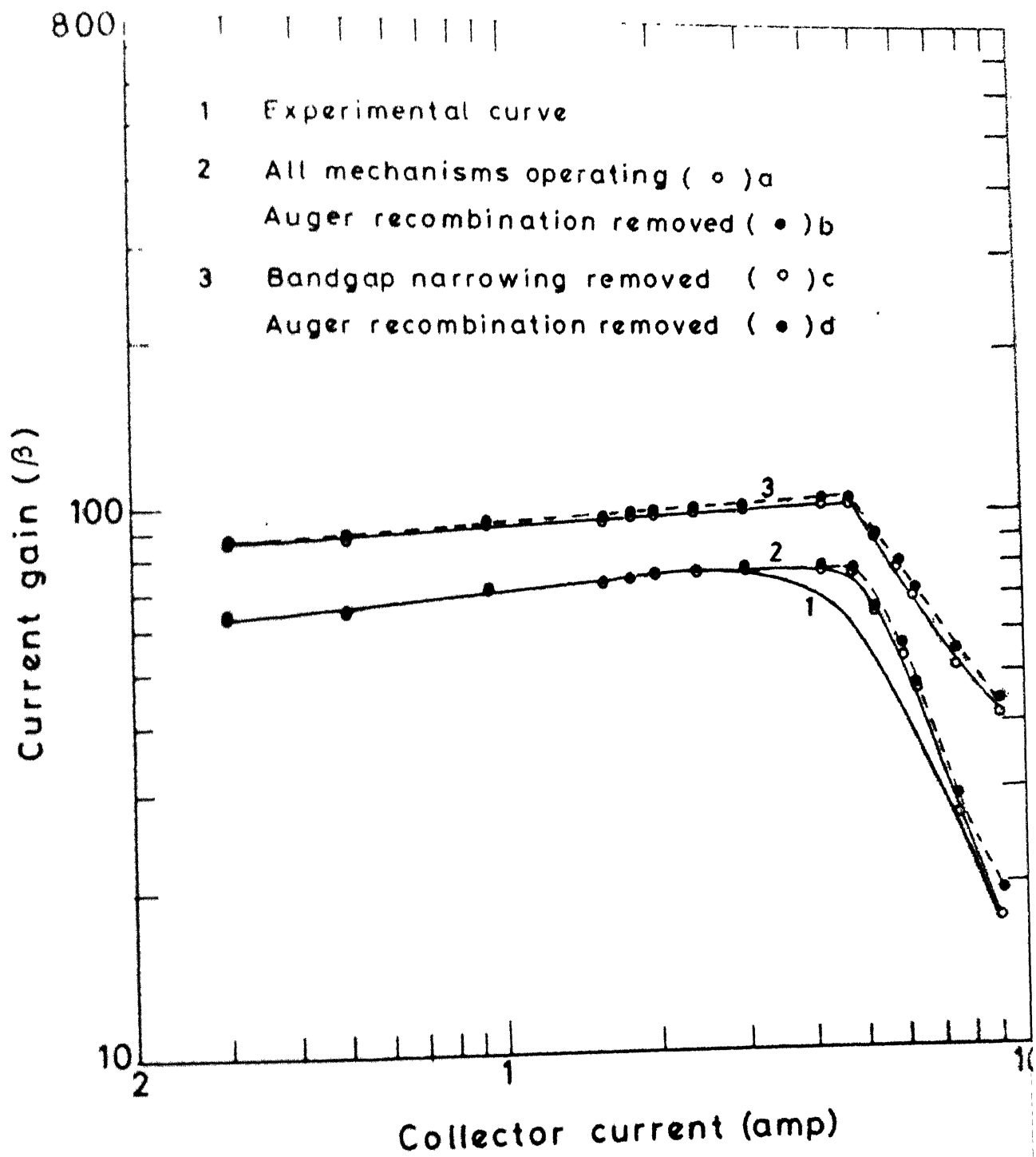


Fig.6 Calculated current gain for different collector currents

CHAPTER 5

CONCLUSION

It is shown that the bandgap narrowing and SRH recombination effects are the dominant mechanisms in influencing the current gain in transistors. Bandgap narrowing effects dominate all others in the devices with shallow emitters of junction depths of 2 μm or less. The SRH recombination has the most influence on the current gain of the devices with emitters of 4 μm or greater. Auger recombination does not appear to be an important mechanism at the low and moderate injection levels. This is dominated by either bandgap narrowing or SRH recombination and cannot explain the observed current gain in the absence of the above two mechanisms. These conclusions have been arrived at by choosing specific values for the parameters governing the physical mechanisms, for example, bandgap narrowing. The specific choice, however will only effect the results for very small emitter depths since recombination prevents the minority carrier from reaching the portion of the emitter doped at this level for the deeper emitter ($\geq 4\mu\text{m}$).

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Appendix

- Programme No.1 - Solves the device equations
- Programme No.2 - Calculates the emitter surface concentration for different junction depths.

```

PROGRAM NO.1
THIS PROGRAM DETERMINES THE COMMON EMITTER CURRENT GAIN FOR AN
NPN POWER TRANSISTOR AFTER SOLVING THE BASIC SEMICONDUCTOR
TRANSPORT EQUATIONS USING FINITE DIFFERENCE METHOD, GUMMEL'S
ALGORITHM AND CROUT'S FACTORISATION METHOD.
VARIABLE DECLARATION
REAL VI, LD, NI, DO, MU, JO, TO, AA, VA, NE, NB, NC, ALPHA, BETA, H1, H2, XE, XB,
1XC, DDP(900), ENI(900), SI(900), PHIP(900), PHIN(900), PHP(900), PHN(9
200), E(900), P(900), B(900), C(900), D(900), S(900), DEL(900), DELMX, DE
3LMN, EF(900), R1(900), R2(900), MUP(900), MUN(900), G(900), JN(900), JP
4(900), HFE, EPS1, X(900)
INTEGER I, J, IT1, Z
OUTPUT FILE
OPEN(UNIT=30, DEVICE='DSK', FILE='PP.1')
NORMALISATION FACTORS
VT=0.026
LD=34.E-4
NI=1.5E10
DO=1.
MU=38.65
JO=7.E-7
TO=34.E-4
AA=LD*5
APPLIED BIAS
VA=0.0
ITERATION STOPPING CRITERIA
IT1M=200
EPS1=0.1E-04
CONSIDERATION OF DIFFERENT MECHANISMS
Z=1 FOR NOMINAL CASE
Z=2 FOR AR REMOVED
Z=3 FOR BGN REMOVED
Z=4 FOR BGN+AR REMOVED
Z=5 FOR EMITTER SRH REMOVED
Z=1
DOPING PROFILE PARAMETERS
NE=(7.E+19)/NI
NB=(2.E+17)/NI
NC=(2.E14)/NI
BETA=1.2
ALPHA=ALOG(NE/(NB*EXP(-BETA)-NC))
XE=(4.75E-4)/LD
XB=(12.25E-4)/LD
XC=(90.E-4)/LD
STEP DISTRIBUTION
  
```

```

H1=(0.1E-4)/LD
H2=H1*H1
N=X2/H1+1
DO 10 I=1,N
  X(I)=I*H1
10 CONTINUE
C1 INITIALISATION OF VARIABLES
DO 20 I=1,N
  DEL(I)=0.0
  PHIP(I)=1.0
  PHIN(I)=1.0
20 CONTINUE
CALL DOPING(N,NE,NB,NC,ALPHA,BETA,XE,X,DOP)
CALL NIEFF(N,VT,Z,NI,DOP,EVI)
CALL SIINT(N,ENI,DOP,SI)
IT1=1
405 CALL COEFF1(N,H2,VA,PHIP,PHIN,SI,DOP,B,C,D,Q)
CALL CROUT(N,B,C,D,Q,DEL)
CALL DLM(N,SI,DEL,DELMX,DELMN)
IF(DELMX.LT.0.1E-04)GO TO 420
IF(IT1.EQ.IT1M) GO TO 430
DO 410 J=1,N
  SI(J)=SI(J)+DEL(J)
410 CONTINUE
  IT1=IT1+1
  GO TO 405
420 WRITE(30,9000)IT1;GO TO 440
430 WRITE(30,910)IT1M
440 DO 450 I=1,N
  SI(I)=SI(I)+DEL(I)
450 CONTINUE
500 CALL PHI(N,PHIP,PHIN,NI,SI,P,E,PHP,PHN)
CALL ELFD(N,H1,VA,SI,EF)
CALL RSRH(N,H1,XE,Z,P,E,NI,R1)
CALL RAGR(N,P,E,NI,R2)
CALL MOBLY(N,MU,DOP,EF,MUP,MUN)
CALL HFG(N,P,E,MUP,MUN,EF,G)
CALL COEFF2(N,H2,VA,Z,MUP,SI,R1,R2,G,B,C,D,Q)
CALL CROUT(N,B,C,D,Q,PHIP)
CALL COEFF3(N,H2,VA,Z,MUN,SI,R1,R2,G,B,C,D,Q)
CALL CROUT(N,B,C,D,Q,PHIN)
CALL PHI(N,PHIP,PHIN,NI,SI,P,E,PHP,PHN)
CALL CRNIS(N,H1,VA,MUP,MUN,PHP,PHN,P,E,JN,JP)
CALL GAIN(N,JP,JN,R1,R2,X,HFE);WRITE(30,*)HFE
200 STOP
9000 FORMAT(10X,'POTENTIAL VALUES CONVERGED AFTER',I3,'ITERATIONS')
910 FORMAT(10X,'NO REQUIRED CONVERGENCE AFTER',I3,'ITERATION')
END
C1 THIS SUBROUTINE DETERMINES DOPING PROFILE

```

```

SUBROUTINE DOPING(N,NE,NB,NC,ALPHA,BETA,XE,X,DOP)
DIMENSION DOP(N),X(N),E1(900),E2(900)
REAL NE,NB,NC
DO 10 I=1,N
E1(I)=ALPHA*((X(I)/XE)**2)
IF(E1(I).GE.20) GO TO 20
E2(I)=BETA*((X(I)/XE)**2)
DOP(I)=NE*EXP(-E1(I))+NC-NB*EXP(-E2(I))
GO TO 10
20 E2(I)=BETA*((X(I)/XE)**2)
IF(E2(I).GE.20) GO TO 30
DOP(I)=-NB*EXP(-E2(I))+NC
GO TO 10
30 DOP(I)=NC
10 CONTINUE
RETURN
END

21 THIS SUBROUTINE DETERMINES BGN CORRECTION FACTOR IN NI
SUBROUTINE NIEFF(N,VT,Z,NI,DOP,ENI)
DIMENSION DOP(N),ENI(N),F(900),ADOP(900)
REAL NI
DO 10 I=1,N
IF(Z.EQ.3) GO TO 30
IF(Z.EQ.4) GO TO 30
XL=(1.E17)/NI
ADOP(I)=ABS(DOP(I))
IF(ADOP(I).GE.XL) GO TO 20
30 ENI(I)=1.
GO TO 10
20 F(I)=ALOG(ADOP(I)/XL)
ENI(I)=EXP((9.E-3)*(F(I)+SQRT(F(I)*F(I)+0.5)))/VT
10 CONTINUE
RETURN
END

21 THIS SUBROUTINE DETERMINES INITIAL VALUE OF ELECTROSTATIC
POTENTIAL (SI)
SUBROUTINE SIINT(N,ENI,DOP,SI)
DIMENSION ENI(N),DOP(N),SI(N)
DO 10 I=1,N
IF(DOP(I).GT.0.0) GO TO 20
SI(I)=-ALOG(-DOP(I))
GO TO 10
20 SI(I)=ALOG(DOP(I))
10 CONTINUE
RETURN
END

21 THIS SUBROUTINE DETERMINES COEFFICIENT MATRIX FOR VARIABLE DEL
SUBROUTINE COEFF1(N,H2,VA,PHIP,PHIN,SI,DOP,B,C,D,Q)
DIMENSION PHIP(N),PHIN(N),SI(N),DOP(N),B(N),C(N),D(N),Q(N)

```



```

DO 10 I=1,N
IF(I.EQ.1) GO TO 20
IF(I.EQ.N) GO TO 30
40 B(I)=-1.0
D(I)=-1.0
C(I)=2.0+H2*(PHIP(I)*EXP(-SI(I))+PHIN(I)*EXP(SI(I)))
Q(I)=-H2*(PHIN(I)*EXP(SI(I))-PHIP(I)*EXP(-SI(I))-DDP(I))+SI(I+1)
I+SI(I-1)-2.0*SI(I)
GO TO 10
20 SI(I-1)=22.263711
GO TO 40
30 SI(I+1)=9.4980224+VA
GO TO 40
10 CONTINUE
RETURN
END
C) THIS SUBROUTINE DETERMINES VALUES OF QUASI-FERMI LEVELS AND
C) CARRIER CONCENTRATIONS
SUBROUTINE PHI(N,PHIP,PHIN,NI,SI,P,E,PHP,PHN)
DIMENSION PHIP(N),PHIN(N),SI(N),P(N),E(N),PHP(N),PHN(N)
REAL NI
DO 10 I=1,N
PHP(I)=ALOG(PHIP(I))
PHN(I)=-ALOG(PHIN(I))
P(I)=NI*EXP(PHP(I)-SI(I))
10 E(I)=NI*EXP(SI(I)-PHN(I))
CONTINUE
RETURN
END
C) THIS SUBROUTINE DETERMINES ELECTRIC FIELD
SUBROUTINE ELFD(N,H1,VA,SI,EF)
DIMENSION SI(N),EF(N)
DO 10 I=1,N
IF(I.EQ.1) GO TO 20
IF(I.EQ.N) GO TO 30
40 EF(I)=-((SI(I+1)-SI(I-1)))/(2.*H1)
GO TO 10
20 SI(I-1)=22.263711
GO TO 40
30 SI(I+1)=9.4980224+VA
GO TO 40
10 CONTINUE
RETURN
END
C) THIS SUBROUTINE DETERMINES SRH RECOMBINATION RATE
SUBROUTINE RSRH(N,H1,XE,Z,P,E,NI,R1)
DIMENSION P(N),E(N),R1(N)
INTEGER J1,Z
REAL NI

```

```

J1=XE/H1
DO 10 I=1,J1
IF(Z.EQ.5)GO TO 50
TNO=5.8E-6
TP0=5.8E-6
GO TO 60
50 TNO=1.5E-4
TP0=1.5E-4
60 R1(I)=(P(I)*E(I)-NI*NI)/(TNO*(P(I)+NI)+TP0*(E(I)+NI))
10 CONTINUE
J11=J1+1
DO 20 I=J11,N
TNO=1.5E-4
TP0=1.5E-4
20 R1(I)=(P(I)*E(I)-NI*NI)/(TNO*(P(I)+NI)+TP0*(E(I)+NI))
CONTINUE
RETURN
END
31 THIS SUBROUTINE DETERMINES AUGER RECOMBINATION RATE
SUBROUTINE RAGR(N,P,E,NI,R2)
DIMENSION P(N),E(N),R2(N)
REAL NI
AN=3.1E-19
AP=2.2E-19
DO 10 I=1,N
10 R2(I)=(AN*E(I)+AP*P(I))*(P(I)*E(I)-NI*NI)
CONTINUE
RETURN
END
31 THIS SUBROUTINE DETERMINES MOBILITIES
SUBROUTINE MOBLTY(N,MU,DOP,EF,MUP,MUN)
DIMENSION DOP(N),EF(N),PMU1(900),EMU1(900),F1(900),
1F2(900),F3(900),G1(900),G2(900),G3(900)
REAL MU,MUP(N),MUN(N)
DO 10 I=1,N
F1(I)=(DOP(I)/((DOP(I)/81.)+2.7E6))
F2(I)=((EF(I)/7.9E2)**2)/((EF(I)/7.9E2)+.21)
F3(I)=((EF(I)/3.2E3)**2)
31 PMU1(I)=1.+F1(I)+F2(I)+F3(I)
31 MUP(I)=1.+(DOP(I)/((DOP(I)/81.)+2.7E5))+(((EF(I)/7.9E2)**2)/((EF
1(I)/7.9E2)+0.21))+((EF(I)/3.2E3)**2)
MUP(I)=((PMU1(I))**(-0.5))*480/39
G1(I)=(DOP(I)/((DOP(I)/350.)+2.E6))
G2(I)=((EF(I)/4.5E2)**2)/((EF(I)/4.5E2)+1.19)
G3(I)=((EF(I)/9.6E2)**2)
31 EMU1(I)=1.+G1(I)+G2(I)+G3(I)
31 EMU1(I)=1.+(DOP(I)/((DOP(I)/350)+2.E5))+(((EF(I)/4.5E2)**2)/((EF
1(I)/4.5E2)+1.15))+((EF(I)/9.6E2)**2)
MUN(I)=((EMU1(I))**(-0.5))*1400/39

```

```

10 CONTINUE
RETURN
END
21 THIS SUBROUTINE DETERMINES HIGH FIELD GENERATION RATE
SUBROUTINE HFG(N,P,E,MUP,MUN,EF,G)
DIMENSION P(N),E(N),MUP(N),MUN(N),EF(N),G(N),ALPHP(900),ALPHN(90
10),AEF(900)
DO 10 I=1,N
AEF(I)=ABS(EF(I))
IF(AEF(I).LT.5250)GO TO 20
ALPHP(I)=7.65E4*EXP(-4.2E5/AEF(I))
ALPHN(I)=1.3E4*EXP(-2.3E5/AEF(I))
G(I)=P(I)*MUP(I)*ALPHP(I)*EF(I)+E(I)*MUN(I)*ALPHN(I)*EF(I)
GO TO 10
20 G(I)=0.0
10 CONTINUE
RETURN
END
21 THIS SUBROUTINE DETERMINES COEFFICIENT MATRIX FOR VARIABLE PHIP
SUBROUTINE COEFF2(N,H2,VA,Z,MUP,SI,R1,R2,G,B,C,D,Q)
DIMENSION MUP(N),SI(N),R1(N),R2(N),G(N),B(N),C(N),D(N),Q(N)
INTEGER Z
DO 10 I=1,N
IF(I.EQ.1) GO TO 20
IF(I.EQ.N) GO TO 30
40 B(I)=-MUP(I)*EXP(-(SI(I)+SI(I-1))/2.0)
D(I)=-MUP(I)*EXP(-(SI(I)+SI(I+1))/2.0)
C(I)=-B(I)-D(I)
IF(Z.EQ.2)GO TO 50
IF(Z.EQ.4) GO TO 50
Q(I)=H2*(R1(I)+R2(I)-G(I))
GO TO 10
50 Q(I)=H2*(R1(I)-G(I))
GO TO 10
20 SI(I-1)=22.263711
GO TO 40
30 SI(I+1)=9.4980224+VA
GO TO 40
10 CONTINUE
Q(1)=Q(1)-B(1)
Q(N)=Q(N)-D(N)*EXP(VA)
RETURN
END
21 THIS SUBROUTINE DETERMINES COEFFICIENT MATRIX FOR VARIABLE PHIN
SUBROUTINE COEFF3(N,H2,VA,Z,MUN,SI,R1,R2,G,B,C,D,Q)
DIMENSION MUN(N),SI(N),R1(N),R2(N),G(N),B(N),C(N),D(N),Q(N)
INTEGER Z
DO 10 I=1,N
IF(I.EQ.1) GO TO 20

```

```

40 IF(I.EQ.N) GO TO 30
   B(I)=-MUN(I)*EXP((SI(I)+SI(I-1))/2.)
   D(I)=-MUN(I)*EXP((SI(I)+SI(I+1))/2.)
   C(I)=-B(I)-D(I)
   IF(Z.EQ.2)GO TO 50
   IF(Z.EQ.4)GO TO 50
   Q(I)=-H2*(R1(I)+R2(I)-G(I))
   GO TO 10
50 Q(I)=H2*(R1(I)-G(I))
   GO TO 10
20 SI(I-1)=22.263711
   GO TO 40
30 SI(I+1)=9.4980224+VA
   GO TO 40
10 CONTINUE
   Q(1)=Q(1)-B(1)
   Q(N)=Q(N)-D(N)*EXP(-VA)
   RETURN
END
21 THIS SUBROUTINE DETERMINES CURRENT DENSITIES
   SUBROUTINE CRNTS(N,H1,VA,MUP,MUN,PHP,PHN,P,E,JN,JP)
   DIMENSION MUP(N),MUN(N),PHP(N),PHN(N),P(N),E(N),JP(N),JN(N)
   DO 10 I=1,N
   IF(I.EQ.1) GO TO 20
   IF(I.EQ.N) GO TO 30
40 JP(I)=-MUP(I)*P(I)*(PHP(I+1)-PHP(I-1))/(2.*H1)
   JN(I)=-MUN(I)*E(I)*(PHN(I+1)-PHN(I-1))/(2.*H1)
   GO TO 10
20 PHP(I-1)=0.0
   PHN(I-1)=0.0
   GO TO 40
30 PHP(I+1)=VA
   PHN(I+1)=VA
   GO TO 40
10 CONTINUE
   RETURN
END
21 THIS SUBROUTINE DETERMINES CURRENT GAIN
   SUBROUTINE GAIN(N,JP,JN,R1,R2,X,HFE)
   DIMENSION JP(N),JN(N),R1(N),R2(N),X(N),R(900)
   REAL HFE,JC,JB
   JC=JP(N)+JN(N)
   DO 10 I=1,N
   R(I)=R1(I)+R2(I)
10 CONTINUE
   CALL DD1GAF(X,R,N,JB,ER,IFAIL)
   IF(IFAIL)40,40,20
20 IF(IFAIL.EQ.1) WRITE(30,*)IFAIL
   IF(IFAIL.EQ.2) WRITE(30,*)IFAIL

```

```

IF(IFAIL.EQ.3) WRITE(30,*) IFAIL
STOP
40 HFE=JC/JB
RETURN
END
21 THIS SUBROUTINE DETERMINES MAX AND MIN CHANGES IN POTENTIALS
SUBROUTINE DLM(N,SI,DEL,DELMX,DELMN)
DIMENSION SI(N),DEL(N)
DELMN=0.0
DELMX=0.0
DO 10 I=1,N
ADEL=ABS(DEL(I))
DELMX=AMAX1(DELMX,ADEL)
DELMN=DELMN+ADEL
10 CONTINUE
DELMN=DELMN/N
RETURN
END
21 THIS SUBROUTINE DETERMINES X BY CROUT'S FACTORISATION METHOD
SUBROUTINE CROUT(N,B,C,D,Q,X)
DIMENSION B(N),C(N),D(N),Q(N),X(N),HM(900),PM(900)
HM(1)=-D(1)/C(1)
PM(1)=Q(1)/C(1)
DO 10 I=2,N
HM(I)=-D(I)/(C(I)+B(I)*HM(I-1))
10 PM(I)=(Q(I)-B(I)*PM(I-1))/(C(I)+B(I)*HM(I-1))
CONTINUE
X(N)=PM(N)
N1=N-1
DO 20 I=1,N1
J=N-I
20 X(J)=PM(J)+HM(J)*X(J+1)
CONTINUE
RETURN
END

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PROGRAM DOCUMENTATION OF FILE : DE IN 2-May-84
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PROGRAM NO.2
THIS PROGRAM DETERMINES EMITTER SURFACE CONCENTRATIONS
REQUIRED FOR EQUAL EMITTER CHARGE FOR DIFFERENT EMITTER DEPTHS
VARIABLE DECLARATION
REAL VT,LD,NI,H1,XE,NE,NB,NC,BETA,ALPHA,X(100),DOP(100),EVI(100)
1,Y(100),QE,ER
INTEGER NN,IFAIL
CONSTANTS DECLARATION
VT=0.026
LD=34.E-4
NI=1.5E10
NJ=38 POINTS CONSIDERED FOR INTEGRATION
NN=99
OUTPUT FILE
OPEN(UNIT=30,DEVICE='DSK',FILE='QE.1')
CONSIDERATION OF DIFFERENT EMITTER DEPTHS
K=1 FOR 1UM EMITTER
K=2 FOR 2UM EMITTER
K=3 FOR 4UM EMITTER
K=4 FOR 4.75UM EMITTER
K=5 FOR 8UM EMITTER
DO 200 K=2,2
IF(K.EQ.1)GO TO 10
IF(K.EQ.2)GO TO 20
IF(K.EQ.3)GO TO 30
IF(K.EQ.4)GO TO 40
IF(K.EQ.5)GO TO 50
XE=(1.E-4)/LD;GO TO 70
XE=(2.E-4)/LD;GO TO 70
XE=(4.E-4)/LD;GO TO 70
XE=(4.75E-4)/LD;GO TO 70
XE=(8.E-4)/LD;GO TO 70
DOPING PROFILE PARAMETERS
NE=(7.E19)/NI
NB=(2.E17)/NI
NC=(2.E14)/NI
BETA=1.2
ALPHA=ALOG(NE/(NB*EXP(-BETA)-NC))
STEP DISTRIBUTION
H1=XE/NN
X(1)=0.0
DO 100 I=1,NN
J=I+1
X(J)=I*H1
CONTINUE

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N=NV+1
DETERMINATION OF DOPING PROFILE
DO 350 I=1,N
DOP(I)=NE*EXP(-ALPHA*((X(I)/XE)**2))-N3*EXP(-BETA*((X(I)/XE)**2)
1)+NC
350 CONTINUE
CALL NIEFF(N,VT,NI,DOP,ENI)
DO 320 I=1,N
Y(I)=DOP(I)/ENI(I)
320 CONTINUE
IFAIL=1
CALL DD1GAF(X,Y,N,QE,ER,IFAIL)
IF(IFAIL)440,440,330
330 WRITE(30,*)IFAIL
440 XE=XE*LD;NE=NE*NI;WRITE(30,*) XE,NE,QE,ER
200 CONTINUE
STOP
END
2] THIS SUBROUTINE DETERMINES BGN CORRECTION TO NI
SUBROUTINE NIEFF(N,VT,NI,DOP,ENI)
DIMENSION DOP(N),ENI(N),F(100),ADOP(100)
REAL NI
DO 10 I=1,N
XL=(1.E17)/NI
ADOP(I)=ABS(DOP(I))
IF(ADOP(I).GE.XL) GO TO 20
30 ENI(I)=1.
GO TO 10
20 F(I)=ALOG(ADOP(I)/XL)
ENI(I)=EXP((9.E-3)*(F(I)+SQRT(F(I)*F(I)+0.5)))/VT
10 CONTINUE
RETURN
END

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